Calculation Policy

EYFS

Number - addition and subtraction

add two single digit numbers

aggregation
Counters on plates







5, 6.

Bead strings or bead bars can be used to illustrate addition including bridging ten by counting on 2 then 3.

5 + 3 = 8

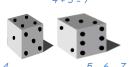


Count on to find the answer

augmentation

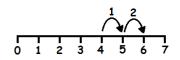
Practically with objects, fingers etc. 5 + 2 "Put 5 in your head, 6, 7."

Dice..



On a prepared number line (start with the bigger number)...

2 + 4 = 6



Number – addition and subtraction subtract two single digit numbers

reduction

Counters on plates



6 take away 1 leaves

1, 2, 3, 4, 5.

Cross out drawn objects to represent what has been taken away:

3 take away 2 is 1



Start with 3 ... 2, 1.

Count on or back to find the answer

Practically, for example:

Group objects on a table then cover some to visualize the calculation:

2 less than 4 is 2



Start with 2... 3, 4.

Coins

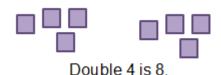


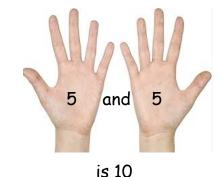
I had 10 pennies. I spent 4 pence. How much do I have left? Start with 10...9, 8, 7, 6.

Number - multiplication and division

solve problems including doubling

Practically double a group of objects to find double of a number by combining then counting the two groups:





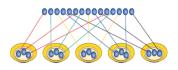
solve problems including halving and sharing

Sharing objects



One for you. One for me...
Is it fair? How many do we each have?

15 shared between 5 is 3.



Grouping objects

Put groups of objects on plates.

How many groups of 4 are there in 12 stars?







understand and use vocabulary for addition

add, more, and, make, sum, total, altogether, score, double, one more, two more, ten more... how many more to make...?

is the same as

understand and use vocabulary for subtraction

take (away), leave, how many are left/left over? how many have gone? one less, two less... ten less... how many fewer is... than...? difference between

is the same as

understand and use vocabulary for multiplication

count on (from, to), count back (from, to), count in ones, twos... tens...

is the same as

understand and use vocabulary for division

half, halve, count out, share out, left, left over

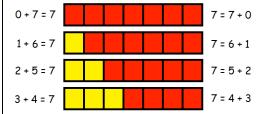
is the same as

Year 1

Number - addition and subtraction

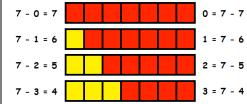
represent and use number bonds up to 20

Start with number bonds to 10 then build. Use a wide range of objects (including fingers!) and images to model the bonds, e.g. interlocking cubes.



represent and use number bond facts related subtraction up to 20

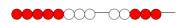
Start with number bonds to 10 then build. Use a wide range of objects (including fingers!) and images to model the bonds, e.g. interlocking cubes.



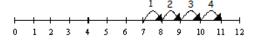
add one-digit and two-digit numbers to 20, including zero

Bead strings or bead bars can be used to illustrate addition including bridging ten by counting on 2 then 3.

8 + 5



On a prepared number line... 7 + 4 = 11



On a hundred square... 3 + 4

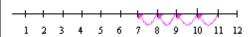
		_/	W	Y	\mathbf{w}	``			
1	2	3	4	Б	6	7	8	9	α
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	उर	38	39	40

subtract one-digit and two-digit numbers to 20, including zero

Practically with objects, fingers etc. 5 - 2 "Put 5 in your head, 4, 3."

Taking away

Number lines (numbered and unnumbered, prepared and child constructed)

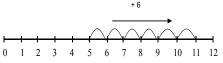


Hundred Square

1	2	3	4	6	6	7	8	9	ю
	12								20
21	22	23	24	26	26	27	28	29	30
31	32	33	34	35	36	उर	38	39	40
	- 0	-			_				

Finding the difference

Number lines (numbered and unnumbered, prepared and child constructed)



Use practical equipment (such as numicon or cuisenaire) to identify the 'difference':



7

'The difference between 7 and 4 is 3' or 'Seven is 3 more than four'.

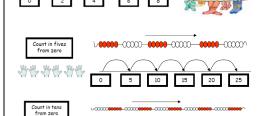
Number - multiplication and division

count in multiples of twos, fives and tens (from number and place value)

Counting using a variety of practical resources

Counting in 2s e.g. counting socks, shoes, animals in the ark... Counting in 10s e.g. hundred square, towers of cubes...

1	2	3	4	Б	6	7	8	9	n
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	BD
51	Б2	63	54	66	56	67	58	B9	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



Use rhymes, songs and stories involving counting on and counting back in ones, twos, fives and tens.
Use 2p, 5p and 10p coins.

double numbers and quantities

(10p) (10p) (10p) (10p)

Practically double a group of objects and/or quantities to find double of a number by combining then counting the two groups.

Progress onto using known facts and counting (in 1s, 2s, 5s and 10s) to double more efficiently.



group and share small quantities

Practical activities involving sharing,

Distributing cards when playing a game, putting objects onto plates, into cups, hoops etc.

Grouping

Sorting objects into 2s / 3s/ 4s etc How many pairs of socks are there?











Sharing pictures /objects

12 children get into teams of 4 to play a game. How many teams are there?







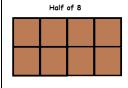
Sweets are shared between 2 people. How many do they have each?

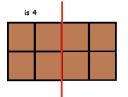
• • • • •

half numbers and quantities

Practically halve objects and/or qualities by sharing them out into two piles and then counting the number of objects in each pile, or cutting/folding pictures of objects in half.

Progress onto using known facts and counting (in 1s, 2s, 5s and 10s) to halve more efficiently.





read, write and interpret mathematical statements involving addition (+) and equals (=) signs

It is important to that children have a clear understanding of the concept of equality, before using the Ξ' sign. Calculations should be on either side of the Ξ' to that children don't misunderstand Ξ' as to mean "the answer".

15 + 2 = 17 15 = 3 + 12 read, write and interpret mathematical statements involving and subtraction (-) equals (=) signs

It is important to that children have a clear understanding of the concept of equality, before using the Ξ sign. Calculations should be on either side of the Ξ' to that children don't misunderstand Ξ' as to mean the answer.

15 - 2 = 13 15 = 18 - 3 make connections between arrays and number patterns

Arrays



Looking at columns 2 + 2 + 2 3 groups of 2

Looking at rows 3 + 3 2 groups of 3

Arrays and repeated addition

4 x 2 or 4 + 4

or 2+2+2+2

There are 4 groups of 3 in 12. 12 shared between 4 is 3.

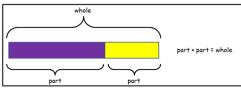
make connections between arrays and number patterns

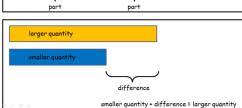
solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 = []+4

To support this, when solving calculations, missing numbers should be placed in all possible places:

Use all the models and images mentioned above. Discuss which is most effective and why.

Singapore Bar Method





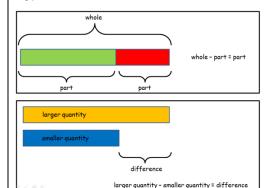
solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 = 1.0

To support this, when solving calculations, missing numbers should be placed in all possible places:

16 - 9 = □ □ = 16 - 9 16 - □ = 7 7 = □ - 9 □ - 9 = 7 7 = 16 - □ □ - ∇ = 7 7 = □ - ∇

Use all the models and images mentioned above. Discuss which is most effective and why.

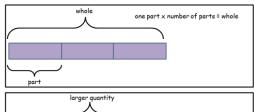
Singapore Bar Method

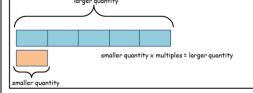


solve one-step problems involving multiplication, by calculating the answer using concrete objects, pictorial representations and arrays with the support

Use all the models and images mentioned above. Discuss which is most effective and why.

Singapore Bar Method





solve one-step problems involving division, by calculating the answer using concrete objects, pictorial representations and arrays with the support

Use all the models and images mentioned above. Discuss which is most effective and why

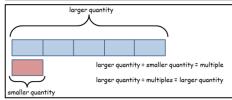
whole + number of parts = one part

whole ÷ one part = number of parts

whole

Singapore Bar Method





understand and use vocabulary for addition, e.g. put together, add, altogether, total and more than

+, add, more, plus, make, total, altogether, score, double, near double, one more, two more... ten more.

= equals, sign, is the same as

How many more to make...? How many more is... than...? How much more is...?

Repetition of facts with different vocabulary:

"What is 2 add 5?"

"What is 2 plus 5?"

What is 2 plus 5?"

What is 4 plus 6?"

understand and use vocabulary for addition and subtraction, e.g. take away, distance between, difference between and less than

- subtract, take (away), minus, leave, how many are left/left over? how many have gone? one less, two less, ten less... how many fewer is... than...? how much less is...? difference between, half, halve, counting up/back...

= equals, sign, is the same as

Repetition of facts with different vocabulary:
"What is 7 take away 37"
"What is 7 subtract 37"
"What is the difference between 3 and 72" etc

use a variety of language to describe multiplication

count on (from, to), count back (from, to), count in ones, twos, threes, fours, fives... count in tens, lots of, groups of, x, times, multiply, multiplied by, multiple of, once, twice, three times... ten times... times as (big, long, wide... and so on), repeated addition, array, row, column, double, halve

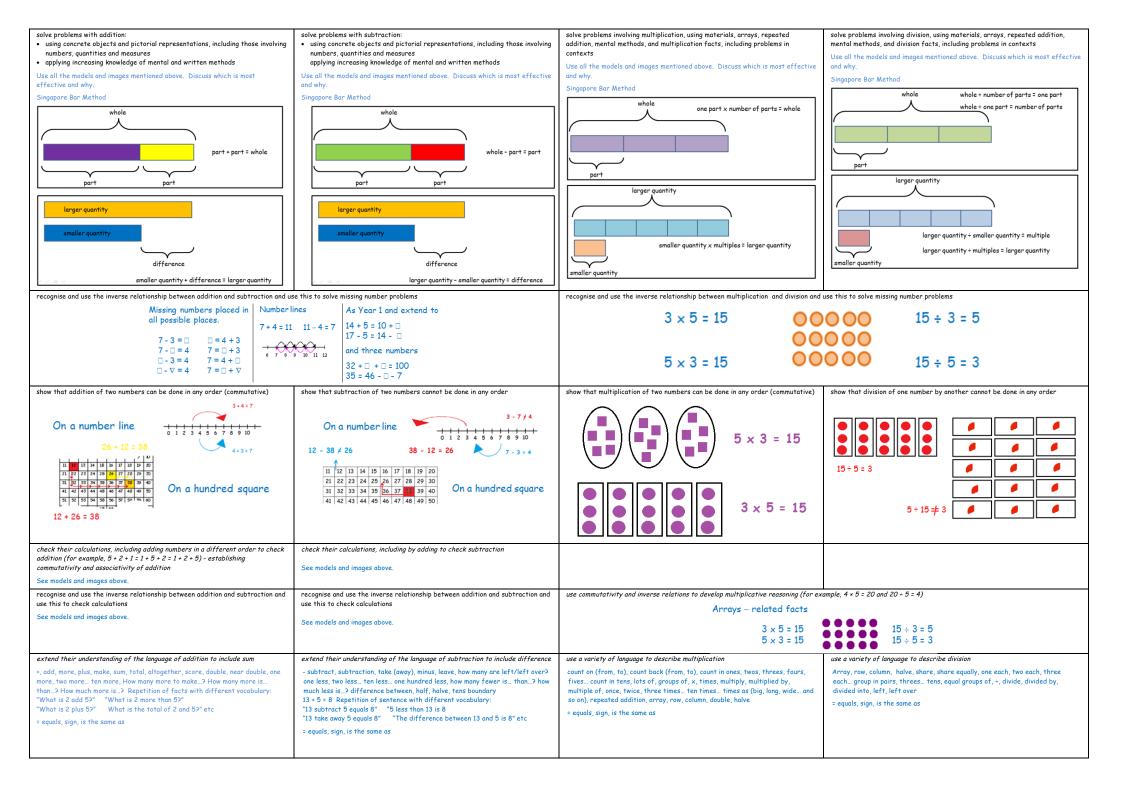
= equals, sign, is the same as

use a variety of language to describe division

Array, row, column, halve, share, share equally, one each, two each, three each... group in pairs, threes... tens, equal groups of

÷, divide, divided by, divided into, left, left over

= equals, sign, is the same as



Year 3

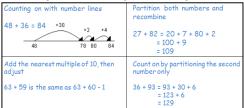
Number - addition and subtraction

add numbers mentally, including:

- a three-digit number and ones
- a three-digit number and tens · a three-digit number and hundreds

Counting on	Adding near numbers and adjusting
115 + 2	433 + 90 = 433 + 100 - 10
	= 533 - 10
"Put 115 in your head, 116, 117."	= 523
Partition number and recombine	Count on by splitting units to make next multiple of ten/hundred
127 + 90 = 100 + 20 + 7 + 90 = 100 + 110 + 7 = 100 + 117 = 217	360 + 80 = 360 + 40 + 40 = 400 + 40 = 440

two two-diait numbers (including answer crossing 100)



- subtract numbers mentally, including:
- · a three-digit number and ones
- · a three-digit number and tens

· a three-digit number and hundreds

Counting back: 263 - 5 "Put 263 in your head, 262, 261, 260, 259, 258." Subtract mentally a 'near multiple

of 10' to or from a two-digit

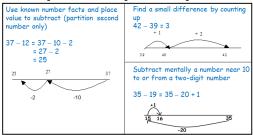
678 - 90 = 678 - 100 + 10

Use unprepared numbered lines t subtract, by counting back:

516 - 400 = 116



two two-digit numbers (including answer crossing 100)



Number - multiplication and division

recall and use multiplication facts for the 3, 4 and 8 multiplication

Play games, chant, test etc to increase speed of recalling facts. Make models and images to display facts.

Investigate patterns within tables.

understand and use mental methods using commutativity and associativity (for example, $4 \times 12 \times 5 = 4 \times 5 \times 12 = 20 \times 12 = 240$)

Use a variety of resources (including a calculator) to investigate order of

Make models and images to display facts.

recall and use division facts for the 3, 4 and 8 multiplication tables

Play games, chant, test etc to increase speed of recalling facts. Make models and images to display facts. Investigate patterns within tables.

understand and use mental methods using multiplication a facts (e.g. using $3 \times 2 = 6$, $6 \div 3 = 2$ and $2 = 6 \div 3$) to derive related facts (e.g. $30 \times 2 = 60.60 \div 3 = 20$ and $20 = 60 \div 3$

$$30 \times 5 = 150$$

$$50 \times 3 = 150$$
 $150 \div 5 = 30$

$$150 \div 5 = 30$$

$$150 \div 3 = 50$$

$$3 \times 5 = 15$$

$$3 \times 5 = 15$$
 $0 \times 5 = 15$ $15 \div 3 = 5$

 $5 \times 30 = 150$

$$15 \div 5 = 3$$

develop reliable written methods for division, starting with

calculations of two-digit numbers by one-digit numbers and

progressing to the formal written methods of short division

add numbers with up to three digits, using formal written methods of columnar addition (See Appendix 1)

Extend mental method of partitioning and recombining. 158 + 72 = 100 + (50 + 70) + (8 + 2) = 100 + 120 + 10 = 230	Vertical expansion 367 +185 12 140 400 552
Column addition 367 +185 552 11	Including money $\begin{array}{c} \text{£ 2.50} \\ + \text{£ 1.75} \\ \underline{\text{£ 4.25}} \\ 1 \end{array}$
Exchange 10 tens for 1 hundred and group with the hundred.	Use base 10 (diennes) or place value counters to support understanding of carrying and to ensure conceptual understanding of place value:

If children are experiencing persistent difficulties.

they could use the partitioned column method with

carrying (using Diennes for support):

200 + 40 + 6

300 + 20 + 2

70 + 6

subtract numbers with up to three digits, using formal written methods of columnar subtraction (See Appendix 1)

Use base 10 (diennes) as a practical method to introduce exchanging

When pupil(s) are confident in doing this practically and verbalizing the calculation, begin to record using partitioned column method:

$$\begin{array}{r}
 20 & 1 \\
 \hline
 30 + 1 \\
 \hline
 -10 + 8 \\
 \hline
 10 + 3
 \end{array}$$

When secure with exchanging, use partitioned column method to solve calculations involving 3 digit numbers. Repeating the practical stage if necessary.

Introduce Column Subtraction without decomposition:

develop reliable written methods for multiplication, starting with calculations of two-digit numbers by one-digit numbers and progressing to the formal written methods of short multiplication

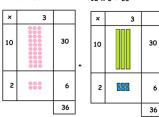
Start by re-enforcing mental methods of partitioning: $13 \times 3 = (10 \times 3) + (3 \times 3)$

Grid Method

1. Introduce the arid method by linking it to arrays initially (using

2. Use base 10 (diennes) 3. Use the grid method: with grid method to support understanding of place value:

 $12 \times 3 = 36$ $12 \times 3 = 36$



How many 3's make 18?

39

× 3

10 30

3 9

Hoops and dots 16 ÷ 2 = 8

Number lines

Move on to calculations that leave remainders and/or require tables knowledge. 1) 16+3=51



When pupils have had experience with and demonstrated understanding of grouping for division, begin to look at short division with no remainders in the final answer.

Hee counters/Diennes to support understanding.

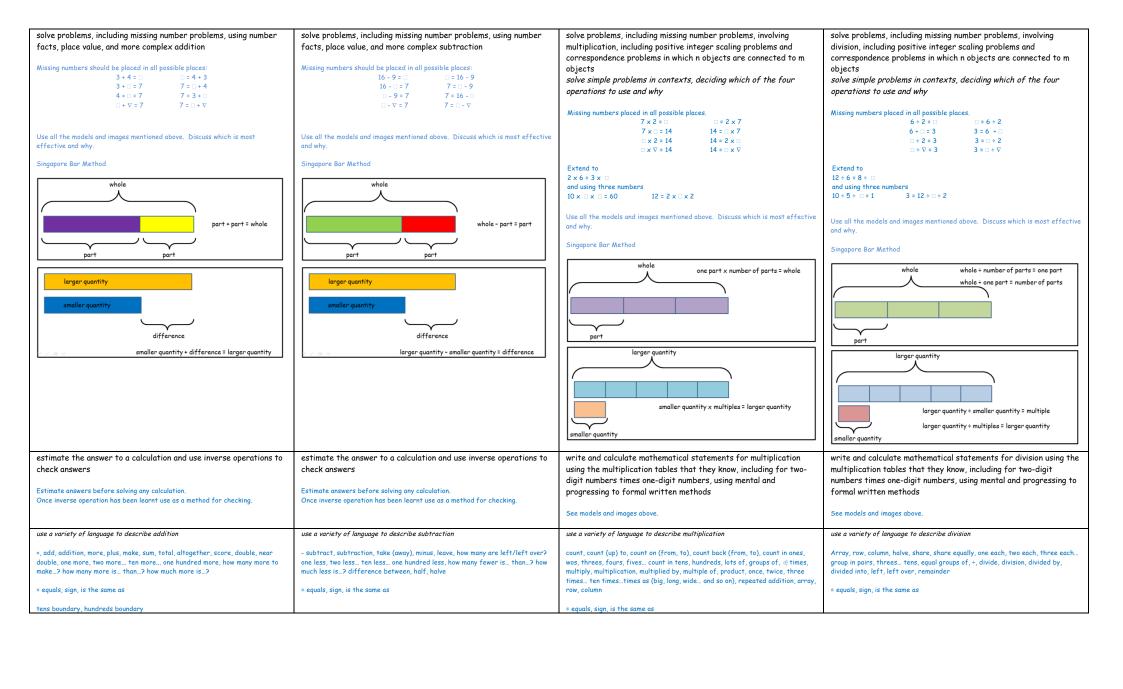
Use counters and a number line

to support pupils understanding.









Year 4

Number - addition and subtraction

add numbers mentally, including:

- · a four-digit number and ones
- a four-digit number and tens · a four-digit number and hundreds

a four-aigit number and thousands	
Counting on	Adding near numbers and adjusting
3115 + 2	7433 + 90 = 7433 + 100 - 10 = 7533 - 10
"Put 3115 in your head, 3116, 3117."	= 7523
Partition number and recombine	Count on by splitting units to make next multiple of ten/hundred
5127 + 2000 = 5000 + 100 + 20 + 7 + 2000 = 7000 + 100 + 20 + 7 = 7127	2360 + 500 = 2360 + 400 + 40 + 60 = 2400 + 400 + 60 = 2860

· three and two-digit numbers

Partition both numbers into hundreds, tens and ones and recombine	Partition second number only into hundreds, tens and ones and recombine
358 + 73 = 300 + 50 + 8 + 70 + 3 = 300 + 120 + 11 = 420 + 11 = 431	358 + 73 = 358 + 70 + 3 = 428 + 3 = 431
Partitioning with number lines +70 +3 358 428 431	Add the nearest multiple of 10 or 100, then adjust 458 + 79 = 458 + 80 - 1

subtract numbers mentally, including

- a four-digit number and ones • a four-digit number and tens
- · a four-digit number and hundreds
- a four-digit number and thousands

Counting back: 5263 - 5

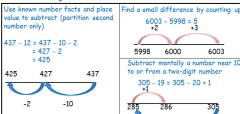
"Put 5263 in your head, 5262, 5261, 5260, 5259, 5258." Subtract mentally a 'near multiple of 10' to or from a two-digit

3678 - 90 = 3678 - 100 + 10

Use unprepared numbered lines to subtract, by counting back: 1516 - 400 = 1116

1116 1216 1316 1416 1516 -100 -100 -100 -100

three and two-digit numbers



subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate (see Appendix 1)

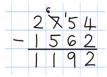
Revision of partitioned column method from Year 3, Moving on to numbers with 4 digits: (use Diennes to support when required.)

	2	フ	5	4	_	ı	5	6	2	=	١	١	9	2
				·		60								
	2	0	0	0	+	7	0	0	+ '	5	0	+	4	
-	1	0	0	0	+	5	0	٥	+	6	0	+	2	
	١	0	0	0	+	١	0	0	+	9	0	+	2	

Column Subtraction without decomposition

Column Subtraction with decomposition

Once pupils are confident in exchanging and have a clear understanding of place value, move towards the formal compact column method: (use Diennes to support when required.)



recall multiplication facts for multiplication tables up to 12 × 12

1E0 - E - 20 1E0 - 2 - E0

Play games, chant, test etc to increase speed of recalling facts. Make models and images to display facts. nvestigate patterns within tables

E0 - 2 - 1E0

use place value, known and derived facts to multiply mentally, including: multiplying by 0 and 1; multiplying together three numbers practise and extend mental methods to three-digit numbers to derive facts, (for

example $600 \div 3 = 200$ can be derived from $2 \times 3 = 6$)

Use knowledge of multiplication facts and place value to derive related facts,

П	30 X 5 = 150	50 x 3 =	150	100 ÷	5 = 50	100 ÷ 3 = 50
╛		$3 \times 5 = 15$	0000	0	15 ÷ 3 = 5	
	3 × 50 = 150		0000	-		150 ÷ 30 = 5
		$5 \times 3 = 15$	0000	0	15 ÷ 5 = 3	
	5 × 30 = 150	50 × 30 =	= 1500	30 x	50 = 1500	150 ÷ 50 = 3

Partition

20 - F - 1F0

$$18 \times 9 = (10 \times 9) + (8 \times 9)$$

= 90 + 72
= 162

ritten layout (see Appendix 1)

 231×7 is approximately $200 \times 10 = 2000$

Grid method

recognise and use commutativity in mental calculations write statements about the equality of expressions (for example, use the distributive law $39 \times 7 = 30 \times 7 + 9 \times 7$ and associative law $(2 \times 3) \times 4 = 2 \times (3 \times 4)$

Use a variety of resources (including a calculator) to investigate order of nultiplication. Make models and images to display facts. multiply two-digit and three-digit numbers by a one-digit number using formal

 $231 \times 7 = 1617$

1400

210

1617

7

200

30

1

nove onto formal method of short multiplication when proficient

Number - multiplication and division recall division facts for multiplication tables up to 12 × 12

Play games, chant, test etc to increase speed of recalling facts. lake models and images to display facts. nvestigate patterns within tables.

use place value, known and derived facts to divide mentally, including: dividing by 1 practise and extend mental methods to three-digit numbers to derive facts. (for example $600 \div 3 = 200$ can be derived from $2 \times 3 = 6$)

lse knowledge of multiplication facts and place value to derive related facts.

$$30 \times 5 = 150$$
 $50 \times 3 = 150$ $150 + 5 = 30$ $150 + 3 = 50$
 $3 \times 5 = 15$ $0 0 0 0$ $15 + 3 = 5$
 $3 \times 50 = 150$ $150 + 30 = 5$
 $5 \times 3 = 15$ $0 0 0 0$ $15 + 5 = 3$
 $5 \times 30 = 150$ $50 \times 30 = 1500$ $30 \times 50 = 1500$ $150 + 50 = 3$

artitioning/Chunking

77 ÷ 5 =
$$(50 \div 5) + (25 \div 5) + (remainder 2)$$

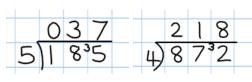
= 10 + 5 + (remainder 2)
= 15 remainder 2

recognise and use factor pairs in mental calculations

Use a variety of resources (including a calculator) to investigate factor pairs. Make models and images to display facts.

divide numbers up to 3 digit by a one-digit number using the formal written method of short division and begin to interpret remainders.

Short division with no remainders in the final answer, use place value counters/Diennes where support is required.



Begin to interpret remainders by looking at word problems to give context and small numbers to start with

Cars carry 5 people. !2 people are going on a trip. How many cars will they







12 ÷ 5 = 2 r 2 So they would need 3 cars

5 buttons are packed in a bag. How many full bags would there be if there were 12 huttons?





 $12 \div 5 = 2 \text{ r 2}$. So there are 2 full bags.

2358 + 373

addition and subtraction where appropriate (see Appendix 1)

add numbers with up to 4 digits using the formal written methods of columnar

2731 11

To ensure conceptual understanding, it is essential that place value is reinforced by frequently

Discussing the actual value of each digit, e.g. the 5 digit represents 5 hundreds.

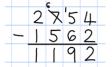
Use base 10 (Diennes) or place value counters to support understanding of carrying and to ensure conceptual understanding of place value (see year 2 and 3 for how to use these manipulatives).

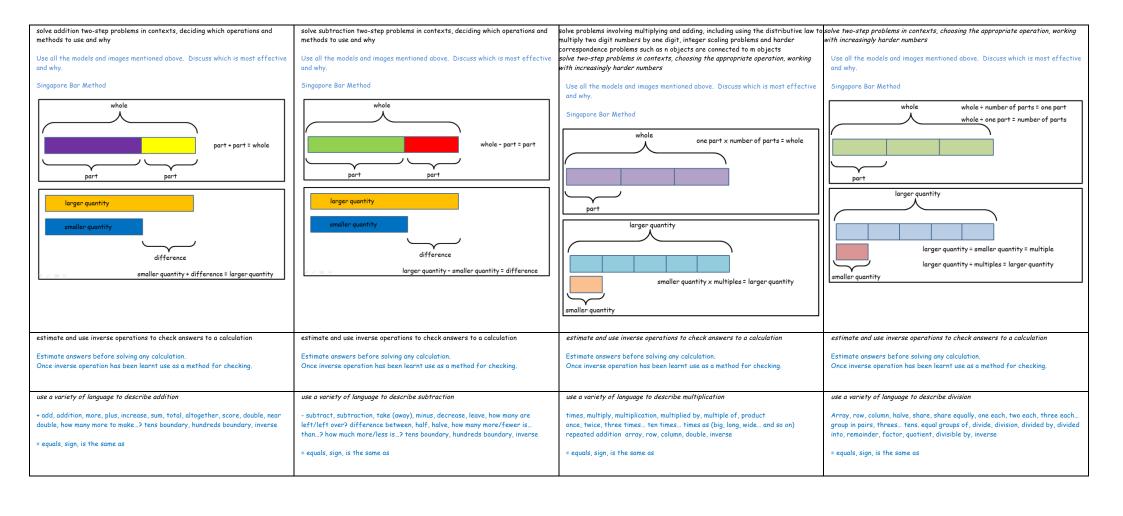
Including decimals

Column addition

To ensure conceptual understanding, it is essential that place value is reinforced by frequently discussing the actual value of each digit, e.g. the 2 digit represents 2 tens.

Use money to support understanding





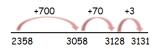
Number - addition and subtraction

add numbers mentally with increasingly large numbers (e.g. 12 462 - 2300 = 10

Partition both numbers and recombine

2358 + 773 = 2000 + 300 + 50 + 8 + 700 + 70 + 3= 2000 + 1000 + 120 + 11 = 3000 + 100 + 30 + 1 =3131

Partitioning with number lines



Partition second number only into hundreds, tens and ones and recombine

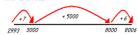
Add the nearest multiple of 10 or 100 then adjust

subtract numbers mentally with increasingly large numbers (e.g. 12 462 - 2300

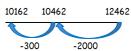
Subtract the nearest multiple of 10 or 100, then adjust

Find a difference by counting up

8006 - 2993 : 5013



Use known number facts and place value to subtract (partition second number only)



add numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction - see Appendix 1)

Column addition

To ensure conceptual understanding, it is essential that place value is reinforced by frequently. Discuss the value of each digit.

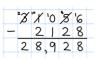
Use base 10 (Diennes) to support understanding of exchanging and to ensure conceptual understanding of place value.

Where there is an 'empty' space in a decimal column, pupils should insert a zero to show the value. Children should be made aware that it is essential to align the columns carefully.

Pupils should be able 3 25 to add more than 2 + 4.13 numbers using the 0.76 compact column 8.14 method.

subtract numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction - see Appendix 1)

Revision of formal compact column method extending to calculations involving numbers with more than 4 digits (use Diennes to support understanding of decomposition and place value).



When confident in using formal compact column method with integers and decimals involving money (always 2 decimal places), extend to subtraction with mixtures of integers and decimals. A clear understanding of place value is essential. Alian the decimal point and use 'place holders' if needed.

Use Diennes or place value counters (add counters with 0.1) to support understanding of decomposition and place value.

Number - multiplication and division multiply numbers mentally drawing upon known facts divide numbers mentally drawing upon known facts

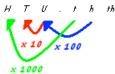
 $47 \times 6 = (40 \times 6) + (7 \times 6)$ =(240)+(42)= 282

Partitioning $72 \div 3 = (60 \div 3) = (12 \div 3)$ = 20 + 4= 24

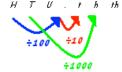
Double and balve

25 x 16 = 50 x 8 = 100 x 4 = 200 x 2 = 400

multiply whole numbers and those involving decimals by 10, 100 and 1000 Place Value



divide whole numbers and those involving decimals by 10, 100 and 1000 Place Value Th H T U . t h th



identify multiples, (and use them to construct equivalence statements, e.g. 4 x $35 = 2 \times 2 \times 35$; $3 \times 270 = 3 \times 3 \times 9 \times 10 = 9^2 \times 10$)

Use a variety of resources (including a calculator) to investigate multiples. Make models and images to display facts.

identify factors, including finding all factor pairs of a number, and common factors of two numbers (and use them to construct equivalence statements, e.g. $4 \times 35 = 2 \times 2 \times 35$: $3 \times 270 = 3 \times 3 \times 9 \times 10 = 9^2 \times 10$

Use a variety of resources (including a calculator) to investigate factors. Make models and images to display facts.

recall prime numbers up to 19 establish whether a number up to 100 is prime

Play games, chant, test etc to increase speed of recalling facts. Make models and images to display facts. Investigate patterns within primes.

recognise and use square numbers and cube numbers, and the notation for squared $\binom{2}{2}$ and cubed $\binom{3}{2}$

Use a variety of resources (including a calculator) to investigate square and cubed numbers. Make models and images to display facts. Investigate the patterns within squared and cubed numbers.

written method, including long multiplication for two-digit numbers

recall prime numbers up to 19 establish whether a number up to 100 is prime

Play games, chant, test etc to increase speed of recalling facts. Make models and images to display facts. Investigate patterns within primes.

multiply numbers up to 4 digits by a one- or two-digit number using a formal

Review formal method of short multiplication (for multiplying by one digit numbers) when proficient

Start with grid method when multiplying by 2 digit

 72×38 is approximately $70 \times 40 = 2800$





Move onto formal long multiplication

X 13

102

Then formal multiplication with more complex numbers:

)	2	3	4	
	×		1	6	
	7	74	0	4	
1	2	143	4	. 0	
	9	,7	4	4	

divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context (as fractions, as decimals or by rounding (for example, 98 ÷ 4 = 98/4 = $24 r 2 = 24 \frac{1}{2} = 24.5 \approx 25)$

Bus shelter method (short division)

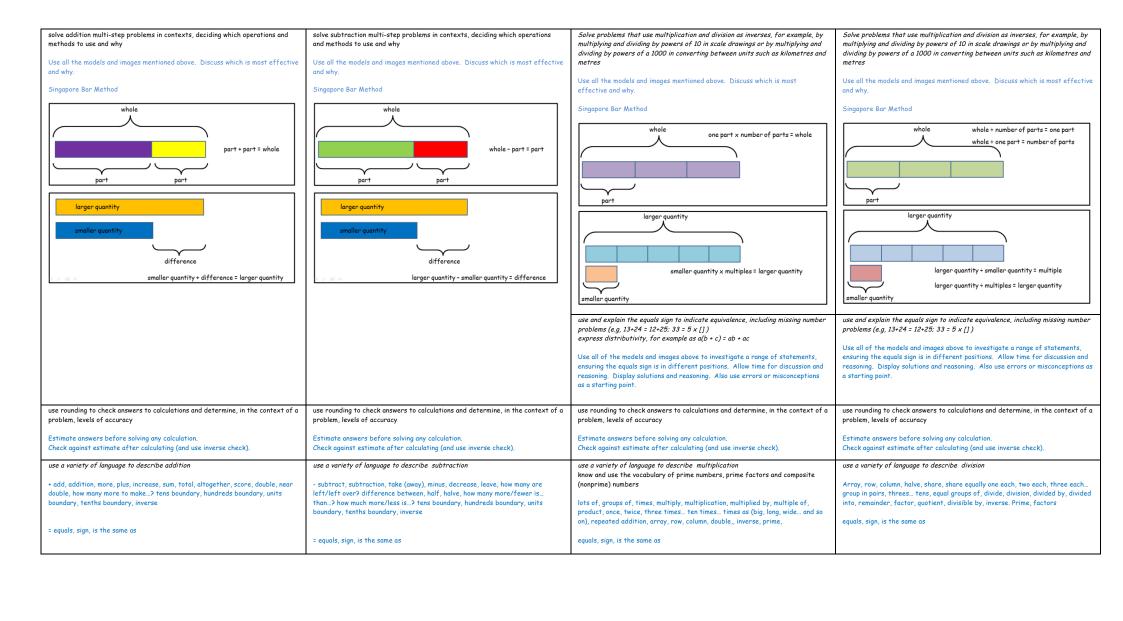
Pupils should consider whether remainders should be left as a reminder rounded to the nearest whole or converted into a decimal or fraction.

Introduce long division (dividing by single digits)

 $256 \div 7$ lies between $210 \div 7 = 30$ and $280 \div 7 = 40$

256
$$\frac{70}{186}$$
 (10 groups) or (10 x 7)
186
 $\frac{140}{46}$ (20 groups) or (20 x 7)
4 (6 groups) or (6 x 7)
4 (36 groups) or (36)

Answer: 36 remainder 4



Number - addition and subtraction

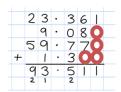
perform mental calculations, including with mixed operations and large numbers (and decimals)

Partition both numbers into hundreds, tens, ones and decimal fractions and recombine

Partition second number only into hundreds, tens, ones and decimal fractions and recombine

Add the nearest whole number then adjust

practise addition for larger numbers, using the formal written methods of columnar addition (see Appendix 1)



Children should be reminded of the importance of alianing the columns accurately.

Where there is an 'empty' space in a decimal column, pupils could insert a zero to show the value.

perform mental calculations, including with mixed operations and large numbers (and decimals)

61 - 24 = 37

Use known number facts and place value to subtract

Subtract the nearest whole number then adjust

practise subtraction for larger numbers, using the formal written

Column Subtraction with decomposition

Number - multiplication and division perform mental calculations, including with mixed operations and large numbers (and decimals)

Partitionina

$$4.7 \times 6 = (4 \times 6) + (0.7 \times 6)$$

= $(24) + (4.2)$
= 282

Double and halve

$$4.25 \times 32 = 8.5 \times 16$$

= 17×8
= 34×4
= 68×2
= 136

identify common factors, common multiples and prime numbers

Use a variety of resources (including a calculator) to investigate common factors, common multiples and prime numbers. Make models and images to display facts. Investigate the patterns within the numbers.

large numbers (and decimals)

Partitionina

$$7.2 \div 3 = (6 \div 3) = (1.2 \div 3)$$

= 2 + 0.4
= 2 4

perform mental calculations, including with mixed operations and

identify common factors, common multiples and prime numbers Use a variety of resources (including a calculator) to investigate

common factors, common multiples and prime numbers. Make models and images to display facts. Investigate the patterns within the numbers

divide numbers up to 4 digits by a two-digit whole number using the formal written method of short and long division, and interpret remainders as whole number remainders, fractions, or by

rounding, as appropriate for the context (Appendix 1)

methods of columnar subtraction (see Appendix 1)

Extend the use of compact column method to adding several numbers with mixed decimals.

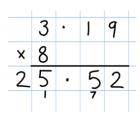


Revision of formal compact column method extending to more complex integers and applying to problem solving using money and measures, including decimals with different numbers of decimal places. Align the decimal point when setting out

Use 'place holders' to aid understanding of the value in that column

multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of short and long multiplication (Appendix 1)

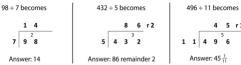
Short multiplication and Long multiplication as in Year 5, but apply to numbers with decimals



Pupils may need reminding that single digits belong in the ones (units) column.

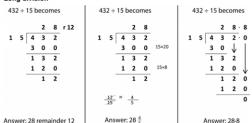
A sound understanding of place value and the formal method itself are required before progressing to decimal multiplication. Short division

Short division



Long division (for dividing by 2 digits)

Long division



Quotients expressed as fractions or decimal fractions

$$61 \div 4 = 15 \frac{1}{2}$$
 or 15.25

solve addition multi-step problems in contexts, deciding which operations and methods to use and why	solve subtraction multi-step problems in contexts, deciding which operations and methods to use and why	solve problems involving multiplication	solve problems involving division
Use all the models and images mentioned above. Discuss which is most effective and why.	Use all the models and images mentioned above. Discuss which is most effective and why.	Use all the models and images mentioned above. Discuss which is most effective and why.	Use all the models and images mentioned above. Discuss which is most effective and why.
Singapore Bar Method	Singapore Bar Method	Singapore Bar Method	Singapore Bar Method
whole part + part = whole	whole - part = part	whole one part x number of parts = whole part	whole + number of parts = one part whole + one part = number of parts part larger quantity
larger quantity smaller quantity difference smaller quantity + difference = larger quantity	larger quantity smaller quantity difference larger quantity - smaller quantity = difference	smaller quantity x multiples = larger quantity smaller quantity	larger quantity ÷ smaller quantity = multiple larger quantity ÷ multiples = larger quantity smaller quantity
round answers to a specified degree of accuracy, e.g. to the nearest 10, 20, 50 etc., but not to a specified number of significant figures	round answers to a specified degree of accuracy, e.g. to the nearest 10, 20, 50 etc., but not to a specified number of significant figures	round answers to a specified degree of accuracy, for example, to the nearest 10, 20, 50 etc., (not to specified number of significant figures)	round answers to a specified degree of accuracy, e.g. to the nearest 10, 20, 50 etc., but not to a specified number of significant figures
Use knowledge of rounding (see fraction Policy) to create estimates.	Use knowledge of rounding (see fraction Policy) to create estimates.	Use knowledge of rounding (see fraction Policy) to create estimates.	Use knowledge of rounding (see fraction Policy) to create estimates.
use their knowledge of the order of operations to carry out calculations involving the four operations explore the order of operations using brackets; for example, $2+1 \times 3 = 5$ and $(2+1) \times 3 = 9$	use their knowledge of the order of operations to carry out calculations involving the four operations explore the order of operations using brackets; for example, $2+1 \times 3 = 5$ and $(2+1) \times 3 = 9$	use their knowledge of the order of operations to carry out calculations involving the four operations explore the order of operations using brackets; for example, $2+1 \times 3 = 5$ and $(2+1) \times 3 = 9$	use their knowledge of the order of operations to carry out calculations involving the four operations explore the order of operations using brackets; for example, $2+1 \times 3 = 5$ and $(2+1) \times 3 = 9$
Review and investigate the effect of carrying out operations in different orders. Explore the effect. Introduce and use BODMAS to solve calculations.	Review and investigate the effect of carrying out operations in different orders. Explore the effect. Introduce and use BODMAS to solve calculations.	Review and investigate the effect of carrying out operations in different orders. Explore the effect. Introduce and use BODMAS to solve calculations.	Review and investigate the effect of carrying out operations in different orders. Explore the effect. Introduce and use BODMAS to solve calculations.
use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy	use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy	use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy	use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy
Estimate answers before solving any calculation. Check against estimate after calculating (and use inverse check).	Estimate answers before solving any calculation. Check against estimate after calculating (and use inverse check).	Estimate answers before solving any calculation. Check against estimate after calculating (and use inverse check).	Estimate answers before solving any calculation. Check against estimate after calculating (and use inverse check).
use a variety of language to describe subtraction	use a variety of language to describe subtraction	use a variety of language to describe subtraction	use a variety of language to describe subtraction
+ add, addition, more, plus, increase, sum, total, altogether, score, double, near double, how many more to make? tens boundary, hundreds boundary, units boundary, tenths boundary, inverse = equals, sign, is the same as	- subtract, subtraction, take (away), minus, decrease, leave, how many are left/left over? difference between, half, halve, how many more/fewer is than? how much more/less is? tens boundary, hundreds boundary, units boundary, tenths boundary, inverse	x lots of, groups of, times, multiply, multiplication, multiplied by, multiple of, product, once, twice, three times ten times times as (big, long, wide and so on), repeated addition, array, row, column double, inverse	Array, row, column, halve, share, share equally one each, two each, three each group in pairs, threes tens, equal groups of, divide, division, divided by, divided into, remainder, factor, quotient, divisible by, inverse
	= equals, sign, is the same as	= equals, sign, is the same as	= equals, sign, is the same as